$\qquad$
Please show all work in the space provided for credit.

1. The graph below represents the graph of a function $P(t)$ where $t$ is the number of years past 1997 and $\mathrm{P}(\mathrm{t})$ is the profit of a small home business. The units on the y -axis are in thousands of dollars. Note that the " $x$-axis" is labeled underneath.

a.) Find $P(6)$. $\qquad$ (This should correspond to a POINT on the graph.)
b.) Now interpret this point. This means that the profit for this business was
\$ $\qquad$ in the year $\qquad$ .
c.) Find $P(12)$. $\qquad$ (This should correspond to a POINT on the graph.)
d.) Now interpret this point. This means that the profit for this business was
\$ $\qquad$ in the year $\qquad$ .
e.) State the intervals of $t$ where the graph is increasing. $\qquad$
f.) Now interpret these intervals.

State the time frames (using the years) where the profit was increasing.

Describe the time frames (using the years) where the profit was decreasing.
g.) State (or approximate) the coordinates of the $x$-intercept(s).
h.) The $\mathbf{x}$-intercepts represent when the business has a profit of \$ $\qquad$
i.) State the domain, using interval notation.

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\#1 continued.
j.) State the range, using interval notation.
k.) The maximum profit was \$ $\qquad$ in the year $\qquad$
I.) The worst year for this company in terms of profit was $\qquad$ when they had a profit of \$ $\qquad$ .
2.) The function $f(x)=27 x^{\frac{1}{3}}$ models the number of plant species, $f(x)$, on an island in terms of the area, $x$, in square miles. What is the area of an island that has 54 species of plants? Show work.
3.) A stone is dropped into a liquid forming circles which increase in radius with time according to the formula $r(t)=4 t$. The area of a circle related to radius is $A(r)=\pi r^{2}$. Using composition of functions, find an equation that would give area as a function of time.

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4.) For $f(x)=3 x^{2}+5$ and $g(x)=7 x-2$,
a. Verify: $g(x+2) \neq g(x)+g(2)$. (The work should be different for each side of the equation.)
b. Find $(f-g)(x)$.
c. Using the resulting function in (b), show that $(f-g)(2)=f(2)-g(2)$.
(The work should be different for each side of the equation.)
d. Is $(f g)(0)=\left(\frac{f}{g}\right)(0)$ ? Explain.
e. Find $\frac{f(x+h)-f(x)}{h}, h \neq 0$. Show work.

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5. The graph of a function $g(x)$ is shown below on a grid.
a.) Fill in the key points for $g(x)$ in the table below.

| $x$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $g(x)$ |  |  |  |  |  |

b.) The function $h(x)=-g(x-5)+4$ involves three transformations on $g(x)$. List the transformations that will be done - in order.
1.) $\qquad$
2.) $\qquad$
3.) $\qquad$
c.) Fill in the table of transformed values for the new graph

| x |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{h}(\mathrm{x})$ |  |  |  |  |  |

d.) Graph $\mathrm{h}(\mathrm{x})$ on the grid below


